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Registry No. ( $\pm$ )-1a, 89908-35-0; ( - )-1a, 69515-17-9; ( $\pm$ )-1b, 89908-41-8; $(R)$-1b $\cdot(S)$ - $\alpha$-methyl- -nitrobenzylamine, $90024-32-1$; ( $S$ )-1b-(S)- $\alpha$-methyl- $p$-nitrobenzylamine, $90024-31-0$; ( $\pm$ )-3, 89908-36-1; ( $\pm$ )-18, 89908-37-2; 19, 22047-88-7; $( \pm)$-20a, 89908-38-3; $( \pm)-20 \mathrm{~b}$,

89908-39-4; (土)-21, 89908-40-7; (土)-22, 89955-26-0; (-)-22, 89955-27-1; ( $\pm$ )-23, 89908-42-9; ( $\pm$ )-24, 89908-43-0; ( $\pm$ )-25, 89908-44-1; ( $\pm$ )-28a, 89908-46-3; ( $\pm$ )-28a (acid), 89908-45-2; ( $\pm$ )-28b, 89908-47-4; ( $\pm$ )-29a, 89908-48-5; ( $\pm$ )-29b, 89908-49-6; ( $\pm$ )-31, 89908-50-9; 34, 89908-56-5; 35, 89908-57-6; 36, 86728-17-8; 37, 89908-51-0; 38a, 89908-52-1; 38b, 89908-54-3; 39a, 89908-53-2; 39b, 89908-55-4; 42, 89955-28-2; 43, 89908-58-7; 44a, 89908-59-8; 44b, 89908-61-2; 45a, 89955-29-3; 45b, 89955-30-6; 46, 89908-60-1; 47, 89908-62-3; PhSeCl, 5707-04-0; cyclohexanone, 108-94-1; 4-methylcyclohexanone, 589-92-4; $(S)-(-)-\alpha$-methyl $-p$-nitrobenzylamine, 4187-53-5.

# Energy-Transfer Study of a Triplet Exciplex of Cyclohexanone and Mesitylene 

Thérèse Wilson, ${ }^{*}$ Stephen L. Frye, ${ }^{\dagger}$ and Arthur M. Halpern ${ }^{\dagger}$<br>Contribution from the Biological Laboratories, Harvard University, Cambridge, Massachusetts 02138. Received October 3, 1983


#### Abstract

Triplet cyclohexanone associates ( $k_{\mathrm{EA}} \sim 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ ) with mesitylene to form a triplet exciplex, $\mathrm{E}^{*}$, with a lifetime of $\sim 0.3 \mu$ s in cyclohexane at $20^{\circ} \mathrm{C}$, i.e. half that of the uncomplexed triplet ketone. This conclusion rests on evidence obtained from energy-trasnfer experiments with 9,10-dibromoanthracene (DBA) as energy acceptor in a formal triplet-singlet energy-transfer process which populates DBA $\left(S_{1}\right)$. In degassed cyclohexane solutions of cyclohexanone ( 0.077 M ), DBA $\left(0.5-5.0 \times 10^{-4}\right.$ M ), and mesitylene ( $0.07-1.0 \mathrm{M}$ ), both $\mathrm{E}^{*}$ and the uncomplexed triplet alkanone sensitize the fluorescence of DBA; its intensity decay is studied by the time-correlated single-photon counting method following pulse excitation at 305 nm where both cyclohexanone and DBA absorb. In the presence of mesitylene, the DBA fluorescence decay profiles reveal the buildup of an excited transient, which is postulated to be the triplet exciplex. The decay curves can be fitted to triple-exponential functions, as predicted by a kinetic scheme based on the reversible formation of $E^{*}$. Kinetic expressions derived from this scheme allow the calculation of all the rate constants of the scheme. At $20^{\circ} \mathrm{C}$, the equilibrium constant favors the exciplex ( $K_{\mathrm{E}} \sim 13$ ). The efficiency $\phi_{\mathrm{TS}}{ }^{\mathrm{E}}$ of the overall triplet-singlet energy transfer from $\mathrm{E}^{*}$ to DBA is $\sim 7$ times higher than from the triplet alkanone; this result is in line with an earlier finding in the case of the less stable triplet exciplex of acetone and benzene. Work is in progress to ascertain the origin of the low $k_{\mathrm{EA}}$, to investigate the effects of solvent and substitution on this rate and on $K_{\mathrm{E}}$, and to investigate the mechanism of TS transfer to DBA.


In contrast to singlet exciplexes, triplet exciplexes in fluid solution have remained largely elusive. ${ }^{1}$ Like any other triplet species, they can be expected to be poor emitters at best; thus, only indirect arguments are, by and large, available for proposing their likely intermediacy in reactions. ${ }^{2}$ It has recently been shown ${ }^{3}$ that exciplexes of triplet alkanones and benzene or methyl-substituted derivatives can be intercepted by 9,10 -dibromoanthracene (DBA), which acts as a unique fluorescence probe. ${ }^{4}$ Energy transfer from the triplet donors populates DBA ( $\mathrm{S}_{1}$ ) of 2-ns lifetime, possibly via a higher triplet state of DBA. Consequently, the intensity decay profile of the resulting fluorescence of DBA contains information on the triplet donors. The fluorescence of DBA has a maximum at $\sim 430 \mathrm{~nm}$ and is easily monitored as a function of time by the single-photon counting technique. ${ }^{4 b}$ This DBA method first revealed the presence of an exciplex of triplet acetone in benzene in dynamic equilibrium with its components, in solutions irradiated at $305 \mathrm{~nm} .^{3 a}$ This result showed conclusively that the much reduced lifetime of triplet acetone in benzene, which is 10 times shorter than in cyclohexane and 1000 times shorter than in acetonitrile, can be regarded as the result of weak complexation. The triplet exciplex which results from the association of a more substituted alkanone such as cyclohexanone with oxylene, for example, was shown to be significantly more stable at room temperature, judging by the three-component fluorescence decay of DBA in this system. ${ }^{3 b}$

The present paper describes a study of the cyclohexanone/ mesitylene system, in cyclohexane at $20^{\circ} \mathrm{C}$. As in the previous

[^0]Scheme I

work, solutions of the ketone, the aromatic, and DBA were submitted to pulse excitation at a wavelength absorbed by both the

[^1]

Figure 1. Fluorescence decay curve of a degassed cyclohexane solution of cyclohexanone ( 0.077 M ), mesitylene ( 0.96 M ), and 9,10 -dibromoanthracene ( $1.05 \times 10^{-4} \mathrm{M}$ ) at $20^{\circ} \mathrm{C}$; $\lambda_{\text {exc }}=305 \mathrm{~nm}$, fluorescence monitored in $420-500 \mathrm{~nm}$ spectral region; see text. The time scale is 0.416 ns per channel. In (A), the plot shows only one data point in eight, with even spacing between points. The weighted residuals are plotted at the top; the insert shows the autocorrelation function $C(t)$ of these residuals. In (B), all data points are plotted between channels 200 and 600. The full-line is the convoluted "best-fit" triple-exponential function, with the following parameters: $k_{\mathrm{F}}=4.61 \times 10^{8} \mathrm{~s}^{-1}, \lambda_{\mathrm{a}}=4.06 \times 10^{6} \mathrm{~s}^{-1}, \lambda_{\mathrm{b}}$ $=1.28 \times 10^{7} \mathrm{~s}^{-1}, \alpha=221, \beta=-0.938$ (eq 1). The value of $\chi^{2}$ is 1.59 , in the range 200-4096 channel numbers.
ketone and DBA. Figure 1 is a typical triple-exponential decay curve of DBA fluorescence in a degassed solution of mesitylene, cyclohexanone, and DBA; the buildup of an excited transient is evident. A series of such curves obtained at different concentrations of the reactants contains a wealth of information from which all the rate constants pertaining to the formation and dissociation of the exciplex can be extracted.

## Kinetic Scheme and Method

The general Scheme I, where A stands for the alkanone, here cyclohexanone, and B for the benzene derivative, here mesitylene, accounts for all the experimental observations. For simplicity, all unimolecular or bimolecular reactions of triplet alkanone or exciplex not involving DBA, such as the photoreduction of cyclohexanone by the solvent, are lumped together in the pseudo-first-order rate constants $k_{\mathrm{d}}{ }^{\mathrm{A}}$ and $k_{\mathrm{d}}{ }^{\mathrm{E}}$. Furthermore, eventual reactions of, and emission from, ${ }^{3} \mathrm{DBA}^{*}$ are of no consequence here and thus need not be considered.

At each concentration of DBA and the aromatic, Scheme I predicts that the experimental decay curve of DBA fluorescence intensity, $I_{t}$ vs. $t$, can be fitted to a function of the form (see Appendix for complete derivation):

$$
\begin{equation*}
I_{t} \propto \alpha e^{-k_{\mathrm{F}} t}+\beta e^{-\lambda_{a} t}+e^{-\lambda_{\mathrm{b}} t} \tag{1}
\end{equation*}
$$

The three rate parameters $k_{\mathrm{F}}, \lambda_{\mathrm{a}}$, and $\lambda_{\mathrm{b}}$ and the two amplitude ratios $\alpha$ and $\beta$ ( $\beta$ has a negative value) are thus accessible experimentally. The parameter $k_{\mathrm{F}}$ is the rate constant of DBA fluorescence decay ( $\sim 5 \times 10^{8} \mathrm{~s}^{-1}$ ), and $\lambda_{\mathrm{a}}$ and $\lambda_{\mathrm{b}}$ are given by

$$
\begin{equation*}
\lambda_{\mathrm{a}, \mathrm{~b}}=(1 / 2)\left(k_{1}+k_{2}\right) \pm(1 / 2) \sqrt{\left(k_{1}-k_{2}\right)^{2}+4 k_{\mathrm{EA}} k_{\mathrm{AE}}[\mathrm{~B}]} \tag{2}
\end{equation*}
$$

[^2]In this equation, $k_{\mathrm{EA}}$ and $k_{\mathrm{AE}}$ are the two important rate constants concerning the exciplex formation and dissociation, and $k_{1}$ and $k_{2}$ are the rates of decay of the uncomplexed triplet ketone and of the exciplex, respectively:

$$
\begin{gather*}
k_{1}=k_{\mathrm{EA}}[\mathrm{~B}]+k_{\mathrm{ET}}{ }^{\mathrm{A}}[\mathrm{DBA}]+k_{\mathrm{d}}^{\mathrm{A}}  \tag{3}\\
k_{2}=k_{\mathrm{AE}}+k_{\mathrm{ET}}{ }^{\mathrm{E}}[\mathrm{DBA}]+k_{\mathrm{d}}{ }^{\mathrm{E}} \tag{4}
\end{gather*}
$$

Equation 2 can be rearranged to give $k_{1}$ and $k_{2}$ :

$$
\begin{equation*}
k_{1,2}=(1 / 2)\left(\lambda_{\mathrm{a}}+\lambda_{\mathrm{b}}\right) \pm(1 / 2) \sqrt{\left(\lambda_{\mathrm{a}}-\lambda_{\mathrm{b}}\right)^{2}-4 k_{\mathrm{EA}} k_{\mathrm{AE}}[\mathrm{~B}]} \tag{5}
\end{equation*}
$$

It can easily be shown that in a series of experiments at a given concentration of DBA, the product $\lambda_{\mathrm{a}} \lambda_{\mathrm{b}}$ and the sum ( $\lambda_{\mathrm{a}}+\lambda_{\mathrm{b}}$ ) should both be linear functions of $[B]$, the concentration of mesitylene, whereas if [B] is kept constant, the plot of ( $\lambda_{\mathrm{a}}+\lambda_{\mathrm{b}}$ ) vs. [DBA] should be linear. Different combinations of rate constants are thus immediately accessible from the slopes and intercepts of these plots (see eq A31, A32 in Appendix).
Because both A and DBA absorb at $\lambda_{\text {exc }}$, i.e., $\left[\text { DBA }^{*}\right]_{0} \neq 0$, the values of the amplitude ratios $\alpha$ and $\beta$ provide a way of determining the efficiencies, $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}$ and $\phi_{\mathrm{TS}} \mathrm{E}$, of triplet-singlet energy transfer, i.e., the fractions of the collisions of DBA and either $A^{*}$ or $E^{*}$ which result in quenching of the donor and concomitant singlet excitation of DBA. If one defines

$$
\begin{align*}
k_{\mathrm{A}} & =\phi_{\mathrm{Ts}}{ }^{\mathrm{A}} k_{\mathrm{ET}}{ }^{\mathrm{A}}[\mathrm{DBA}]  \tag{6}\\
k_{\mathrm{E}} & =\phi_{\mathrm{TS}}{ }^{\mathrm{E}} k_{\mathrm{ET}}{ }^{\mathrm{E}}[\mathrm{DBA}]  \tag{7}\\
Z & =\left(k_{\mathrm{E}} / k_{\mathrm{A}}\right) k_{\mathrm{EA}}[\mathrm{~B}] \tag{8}
\end{align*}
$$

then, with two simplifying assumptions, $k_{F} \gg \lambda_{a}$ and $\alpha \gg 1$ (see below), expressions for $Z$ and for $k_{\mathrm{A}}$ can be derived

$$
\begin{gather*}
Z=\frac{\left(k_{2}-\lambda_{\mathrm{a}}\right)+\beta\left(k_{2}-\lambda_{\mathrm{b}}\right)}{1+\beta}  \tag{9}\\
k_{\mathrm{A}}=\frac{\beta k_{\mathrm{F}} R\left(\lambda_{\mathrm{b}}-\lambda_{\mathrm{a}}\right)}{\alpha\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)} \tag{10}
\end{gather*}
$$

where $R$ is the ratio of absorbances of DBA and the ketone

$$
\begin{equation*}
R=\frac{\epsilon_{\mathrm{DBA}}[\mathrm{DBA}]}{\epsilon_{\mathrm{A}}[\mathrm{~A}]} \tag{11}
\end{equation*}
$$

Thus, if $k_{2}$ has been determined from the experimentally measured $\lambda_{a}$ and $\lambda_{b}$, then $Z$ can be calculated by eq 9 and a plot of $Z$ vs. [ B ] should be linear, according to eq 8 . Note, however, that since $\beta$ is negative, the error on $Z$ becomes prohibitively large as $\beta$ tends to -1 , at high values of [B].

In the absence of mesitylene and therefore of exciplex, the simplified reaction scheme ${ }^{3 \mathrm{a}}$ predicts that the DBA fluorescence decay curves will be double exponentials, of the form

$$
\begin{equation*}
I_{t}=\alpha e^{-k_{\mathrm{F} t} t}+e^{-k_{\mathrm{obsa}} t} \tag{12}
\end{equation*}
$$

where

$$
\begin{equation*}
k_{\mathrm{obsd}}=k_{\mathrm{d}}^{\mathrm{A}}+k_{\mathrm{ET}}^{\mathrm{A}}[\mathrm{DBA}] \tag{13}
\end{equation*}
$$

The efficiency $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}$ is then given by

$$
\begin{equation*}
\phi_{\mathrm{TS}}{ }^{\mathrm{A}}=\frac{R\left(k_{\mathrm{F}}-k_{\mathrm{obsd}}\right)}{(1+\alpha) k_{\mathrm{ET}}{ }^{\mathrm{A}}[\mathrm{DBA}]} \tag{14}
\end{equation*}
$$

with $R$ defined as in eq $11 .^{7}$
Thus, the rate constants $k_{\mathrm{d}}{ }^{\mathrm{A}}$ and $k_{\mathrm{ET}}{ }^{\mathrm{A}}$ and the efficiency $\phi_{\mathrm{Ts}}{ }^{\mathrm{A}}$ can be independently obtained from a series of experiments with solutions of A and DBA only.

## Experimental Section

The fluorescence decay curves were obtained by the time-correlated single-photon counting method. Preliminary work on this system was
(7) Equation 14 is identical with eq 23 in ref 4 b , since $N_{\mathrm{p}}^{\prime} / N_{\mathrm{s}}^{\prime}=k_{\mathrm{obsd}} / k_{\mathrm{F}}$.
done at Northeastern University, on an instrument previously described. ${ }^{4 \mathrm{~b}, 8}$ The results presented here were obtained at Harvard Universtiy with a setup consisting of a PRA lamp housing and deuteri-um-filled lamp, sample chamber and photomulitplier tubes, a Bausch and Lomb high intensity monochromator with adjustable entrance and exit slits on the exciting beam, Ortec electronics, and a Tracor-Northern TN-7200 multichannel analyzer. The vacuum-degassed samples were contained in $1-\mathrm{cm}^{2}$ quartz cells and their temperature $\left(20^{\circ} \mathrm{C}\right)$ controlled by a thermoelectric Peltier device ( $\pm<0.3^{\circ} \mathrm{C}$ ). The fluorescence emission was filtered through a combination of a wide-band interference filter and a cutoff filter (resulting $1 / 2$ bandwidth $=70 \mathrm{~nm}$, centered at $\sim 450$ $\mathrm{nm}, 50 \%$ peak transmittance). Excitation was at 305 nm ( $15-\mathrm{nm}$ bandpass) where $\epsilon_{A}=12.2$ and $\epsilon_{\text {DBA }}=180$ in cyclohexane, the solvent throughout. At least $90 \%$ of the exciting light was therefore absorbed by the ketone (concentration 0.077 M ) and at most $10 \%$ by DBA (concentration range $0.5-5 \times 10^{-4} \mathrm{M}$ ). At 305 nm , the extinction coefficient of mesitylene is $3.5 \times 10^{-2} \mathrm{M}$; at its highest concentration ( 1 M ), the partial absorbance of mesitylene is thus about $3.5 \%$ of that of cyclohexanone.

The full 4096-channel capability of the TN-7200 was used throughout. With such a large number of channels, it was necessary to acquire only one decay curve per sample, on one time scale, in order to determine accurately the slow decay components ( $\tau \sim 0.5 \mu \mathrm{~S}$; see Figure 1) and yet have completely adequate resolution of the first fast peak ( $\tau \sim 2 \mathrm{~ns}$ ) as well as an unambiguous estimate of the amplitude ratios. In fact, a high resolution is a prerequisite for a meaningful analysis of the decay profiles obtained in this work.

The wide excitation band-pass ( 15 nm ) was selected in order to minimize the necessary acquisition time; $1-2 \mathrm{~h}$ was standard. The width of the band-pass does not affect the determination of the three decay rates $k_{\mathrm{F}}, \lambda_{\mathrm{a}}$, and $\lambda_{\mathrm{b}}$, hence of any of the rate constants of Scheme I, except $k_{\mathrm{A}}$ and $k_{E}$ (eq 6,7), although the ratio $k_{E} / k_{A}$ is also independent of the excitation band-pass. In contrast, the ratio of absorbances $(R)$ (eq 11) enters in the calculation of $k_{\mathrm{A}}$ (eq 10 ), hence of $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}$; here the $15-\mathrm{nm}$ excitation band-pass may introduce an error of a factor of $\$ 2$, with the true value of $\phi_{T S}{ }^{A}$ being higher than the experimental value. To obviate this difficulty, a narrow band-pass ( 1.6 nm ) was used to determine $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}$ according to eq 14 , in cyclohexane solutions of cyclohexanone and DBA only, without mesitylene.

A lamp profile was acquired either immediately before or after each fluorescence decay curve. The data (lamp and fluorescence curves) were stored on a PDP 11 / 10 prior to analysis on a VAX by an iterative reconvolution program developed at Northeastern University. The quality of the fit was judged by the values of $\chi^{2}$ over the whole time range and by the standard deviations on each parameter of the three-exponential functions, the randomness of the residuals, and the autocorrelation function along the time axis ${ }^{9}$ as well as, importantly, by qualitative visual judgement on the CRT screen.

Absorption spectra and extinction coefficients were obtained with a Uvikon 820 (KONTRON) spectrophotometer, and the fluorescence spectra with a Perkin-Elmer MPF-44 spectrofluorimeter. Cyclohexane was from Burdick and Jackson ("distilled in glass"); 9,10-dibromoanthracene (Aldrich) was recrystallized from xylene and vacuum sublimed; mesitylene (Fisher) and cyclohexanone (Eastman) were redistilled.

## Results

1. Decay Rates. The kinetic scheme predicts that the formation of an exciplex of triplet cyclohexanone and mesitylene, in irradiated solutions containing DBA, will result in DBA fluorescence decay curves describable by the sum of three exponentials, of which one has a negative coefficient ( $\beta$ in eq 1 ), provided that the exciplex can sensitize DBA fluorescence and that its dissociation is slow compared to other modes of deactivation. The validity of this prediction was verified for all the cyclohexane solutions of cyclohexanone $(0.076 \mathrm{M})$, DBA $\left(0.5-5.0 \times 10^{-4} \mathrm{M}\right)$, and mesitylene ( $0.07-1.0 \mathrm{M}$ ) studied here. In all cases, the emission is DBA fluorescence, with only negligible contributions from cyclohexanone fluorescence and phosphorescence.

Of the three decay parameters, one is larger than the others by 2 orders of magnitude; it is also independent of the concentrations of mesitylene and DBA. This is $k_{\mathrm{F}}\left(\sim 4.7 \times 10^{8} \mathrm{~s}^{-1}\right)$. The two other decay parameters, $\lambda_{a}$ and $\lambda_{b}$, increase with the concentrations of mesitylene and DBA, which means that neither $\lambda_{\mathrm{a}}$ nor $\lambda_{\mathrm{b}}$ can be identified with $k_{1}$ or $k_{2}$, since $k_{2}$, eq 4 , should be
(9) Grinvald, A.; Steinberg, I. Z. Anal. Biochem. 1974, 59, 583.


Figure 2. Plots of $k_{1}$ and $k_{2}$, as defined by eq 3 and 4 , as a function of the concentration of mesitylene in degassed cyclohexane at $20^{\circ} \mathrm{C}$. The concentrations of cyclohexanone and DBA were 0.077 M and $1.05 \times 10^{-4}$ M , respectively. The values of $k_{1}$ and $k_{2}$ were calculated according to eq 25, with an arbitrary value of $k_{\mathrm{EA}} k_{\mathrm{AE}}=9 \times 10^{12} \mathrm{M}^{-1} \mathrm{~s}^{-2}$ (see text). The slope of $k_{1}$ vs. [B] is $1.09 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, and the intercept is 1.87 $\times 10^{6} \mathrm{~s}^{-1}$ (linear regression through all points, $\tau=0.950$ ). The average value of $k_{2}$ is $4.7 \times 10^{6} \mathrm{~s}^{-1}$.
independent of [B]. For a series of solutions at constant concentration of DBA and increasing concentrations of mesitylene, the values of $k_{1}$ and $k_{2}$ can, however, be derived from $\lambda_{a}$ and $\lambda_{b}$ on the basis of eq 5 , as follows. Arbitrary values are assigned to the product $k_{\mathrm{EA}} k_{\mathrm{AE}}$ (with $k_{\mathrm{EA}} k_{\mathrm{AE}}<\left(\lambda_{\mathrm{a}}-\lambda_{\mathrm{b}}\right)^{2} / 4[\mathrm{~B}]$ ) in eq 5 until a value of this product is found which renders one of $k_{1,2}$ independent of the concentration of mesitylene, i.e., $k_{2}$, while the other, i.e., $k_{1}$, becomes linearly dependent on [B]. A value of $k_{\mathrm{EA}} k_{\mathrm{AE}} \simeq(9 \pm 2) \times 10^{12} \mathrm{M}^{-1} \mathrm{~s}^{-2}$ is best (Figure 2). Note the apparent "crossing" of the rates: at low [B] $\lambda_{\mathrm{a}}$ is close to $k_{2}$ and $\lambda_{\mathrm{b}}$ to $k_{1}$, while at high [ B ] the reverse is true. At a mesitylene concentration of 0.25 M , triplet cyclohexanone and its exciplex with mesitylene have nearly the same lifetimes.

According to eq 3 , the slope of the plot $k_{1}$ vs. [B] (Figure 2) is $k_{\mathrm{EA}}$, the association rate constant for exciplex formation. Least-squares analysis gave

$$
k_{\mathrm{EA}}=1.1 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}
$$

hence $k_{\mathrm{AE}}=(8 \pm 2) \times 10^{5} \mathrm{~s}^{-1}$, if $k_{\mathrm{EA}} k_{\mathrm{AE}}=(9 \pm 2) \times 10^{12} \mathrm{M}^{-1}$ $\mathrm{s}^{-2}$. The intercept of this plot is

$$
k_{\mathrm{d}}^{\mathrm{A}}+k_{\mathrm{ET}}^{\mathrm{A}}[\mathrm{DBA}]=1.9 \times 10^{6} \mathrm{~s}^{-1}
$$

Figure 2 also shows that $k_{2}=(4.7 \pm 1) \times 10^{6} \mathrm{~s}^{-1}$ (eq 4). As will now be shown, further treatment of the data provide support for these results.
2. Estimate of All the Rate Constants of Scheme I. The values of $\lambda_{a}$ and $\lambda_{b}$ were determined for two series of solutions at constant cyclohexanone concentration ( 0.076 M ), in which either the mesitylene or the DBA concentration was varied with the other kept constant. The data were analyzed according to eq A31 and A32 (Appendix), and the resulting plots are shown in Figures 3 and 4.

The slope of $\left(\lambda_{\mathrm{a}}+\lambda_{\mathrm{b}}\right)$ vs. [B] is $k_{\mathrm{EA}}=1.1 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, in agreement with the value obtained above from the plot of $k_{1}$ vs. [B]. A host of rate constants, or sums of constants, can immediately be derived from Figures 3 and 4, using eq A31 and 32. They are listed in Table I, along with their sources. For example, the ratio of the slopes of $\lambda_{a} \lambda_{b}$ and of $\left(\lambda_{a}+\lambda_{b}\right)$ vs. $[B]$ is $k_{d}^{E}+$ $k_{\mathrm{ET}}{ }^{\mathrm{E}}[\mathrm{DBA}]=4.4 \times 10^{6} \mathrm{~s}^{-1}$ (Figure 3 and eq A31, A32, Appendix). Combined with $k_{2}=4.7 \times 10^{6} \mathrm{~s}^{-1}$, one gets $k_{\mathrm{AE}} \sim 3$ $\times 10^{5} \mathrm{~s}^{-1}$. This is lower than the value of $(8 \pm 2) \times 10^{5} \mathrm{~s}^{-1}$ derived

Table I. Rate Constants of Scheme I

| rate constants | entry | estimated value | sources ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: |
| $k_{\text {EA }}$ | 1 a | $1.1 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | slope of $k_{1}$ vs. [B] with arb. $k_{\mathrm{EA}} k_{\mathrm{AE}}=9 \times 10^{12} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ (eq 4, 5, Figure 2) |
|  | 1b | $1.1 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | slope of ( $\lambda_{a}+\lambda_{b}$ ) vs. [B] (eq A32, Figure 3) |
| $k_{\text {AE }}$ | 2a | $8 \times 10^{5} \mathrm{~s}^{-1}$ | from $k_{\mathrm{EA}} k_{\mathrm{AE}}=9 \times 10^{12} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ with 1a |
|  | 2b | $3 \times 10^{5} \mathrm{~s}^{-1}$ | from ratio of slopes of $\lambda_{a} \lambda_{b}$ and ( $\lambda_{a}+\lambda_{b}$ ) vs. [B], with 3 a (eq A31, A32, and 4) |
| $k_{2}=k_{\mathrm{d}}{ }^{\mathrm{E}}+k_{\mathrm{AE}}+k_{\mathrm{ET}}{ }^{\mathrm{E}}[\mathrm{DBA}]$ | 3a | $4.7 \times 10^{6} \mathrm{~s}^{-1}$ | from eq 5 with $k_{\mathrm{EA}} k_{\mathrm{AE}}=9 \times 10^{12} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ (Figure 2) |
|  | 3b | $4.4-4.8 \times 10^{6} \mathrm{~s}^{-1}$ | from eq 4 with $\mathbf{2 , 6}, 9$ |
| $k_{\mathrm{ET}}{ }^{\text {A }}$ | 4 | $4.5 \times 10^{9} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | slope of $k_{\text {obsd }}$ vs. [DBA] (eq 13) |
| $k_{\mathrm{ET}}{ }_{\mathrm{E}}+k_{\mathrm{ET}}{ }^{\text {A }}$ | 5 | $9.7 \times 10^{9} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | slope of ( $\lambda_{a}+\lambda_{b}$ ) vs. [DBA] (eq A31, Figure 4) |
| $k_{\mathrm{ET}}{ }^{\mathrm{E}}$ | 6 | $5.2 \times 10^{9} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | from 4 and 5 |
| $k_{\text {d }}{ }^{\text {A }}$ | 7 a | $1.7 \times 10^{6} \mathrm{~s}^{-1}$ | intercept of $k_{\text {obsd }}$ vs. [DBA] (eq 13) |
|  | 7b | $1.4 \times 10^{6} \mathrm{~s}^{-1}$ | intercept of $k_{1}$ vs. [B] (eq 3) with 4 |
| $k_{\mathrm{d}}{ }^{\mathrm{A}}+k_{\mathrm{AE}}+k_{\mathrm{d}}{ }^{\mathrm{E}}$ | 8 a | $5.5 \times 10^{6} \mathrm{~s}^{-1}$ | intercept of ( $\lambda_{\mathrm{a}}+\lambda_{\mathrm{b}}$ ) vs. [B] (eq A32, Figure 3) with 5 |
|  | 8b | $5.7 \times 10^{6} \mathrm{~s}^{-1}$ | intercept of ( $\lambda_{a}+\lambda_{b}$ ) vs. [DBA] (eq A32, Figure 4) with 1 |
| $k_{\mathrm{d}}{ }^{\mathrm{E}}$ | 9a | $3.0 \times 10^{6} \mathrm{~s}^{-1}$ | from 2, 7, and 8 |
|  | 9b | $3.4 \times 10^{6} \mathrm{~s}^{-1}$ | from 2, 3a, and 6 |
| $k_{\mathrm{EA}}\left(k_{\mathrm{d}}{ }^{\mathrm{E}}+k_{\mathrm{ET}}{ }^{\mathrm{E}}\right.$ [DBA] $)$ | 10a | $4.9 \times 10^{13} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | slope of $\lambda_{a} \lambda_{b}$ vs. [B] (eq A31, Figure 3) |
|  | 10b | $3.9 \times 10^{13} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | from 1, 6, and 9 |
| $\begin{aligned} & k_{\mathrm{ET}}^{\mathrm{E}} \phi_{\mathrm{Ts}}^{\mathrm{E}} k_{\mathrm{EA}} / k_{\mathrm{ET}}{ }^{\mathrm{A}} \phi_{\mathrm{TS}}{ }^{\mathrm{A}} . \end{aligned}$ | 11 | $8.8 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | slope of $Z$ vs. [B] (eq 6, 7, 8, 9, Figure 5) |
|  | 12a | 0.01 | eq 6 and 10 with 4 |
|  | 12b | 0.01-0.02 | $\text { eq } 14$ |
| $\phi_{\text {Ts }}{ }^{\text {E }}$ | 13 | 0.07-0.15 | from 1, 4, 6, 11, $12(6,7,8)$ |

${ }^{a}$ The boldface numbers refer to the entries in this table.


Figure 3. Plots of $\left(\lambda_{a}+\lambda_{b}\right)$ and of $\lambda_{a} \lambda_{b}$ (as defined in eq 1 ) as a function of the mesitylene concentration, according to eq A31 and A32, for a series of degassed cyclohexane solutions at $20^{\circ} \mathrm{C}$; cyclohexanone concentration $=0.077 \mathrm{M}$, DBA concentration $=1.05 \times 10^{-4} \mathrm{M}$. Leastsquares analysis through all points gave for $\left(\lambda_{a}+\lambda_{b}\right)$ vs. [B], slope $=$ $(1.11 \pm 0.08) \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, intercept $=(6.50 \pm 0.25) \times 10^{6} \mathrm{~s}^{-1}, r=$ 0.986 ; for $\lambda_{\mathrm{a}} \lambda_{\mathrm{b}}$ vs. [B], slope $=(4.9 \pm 0.4) \times 10^{13} \mathrm{M}^{-1} \mathrm{~s}^{-2}$, intercept $=$ $(4.9 \pm 0.3) \times 10^{12} \mathrm{~s}^{-1}, r=0.984$.
above, but given the uncertainties attached to this type of calculations, a value of $k_{\mathrm{AE}} \sim(6 \pm 4) \times 10^{5} \mathrm{~s}^{-1}$ can be accepted quite confidently.

To complete the analysis, a series of degassed solutions of cyclohexanone ( 0.09 M ) and DBA ( $0.5-7.2 \times 10^{-4} \mathrm{M}$ ), without mesitylene, was also studied under the same conditions of solvent and temperature ( $20^{\circ} \mathrm{C}$ ). The fluorescence decay curves were strictly double exponential, in accord with eq 12. The values of $k_{\mathrm{d}}{ }^{\mathrm{A}}$ and $k_{\mathrm{ET}}{ }^{\mathrm{A}}$, obtained from the plot of $k_{\mathrm{obss}} \mathrm{vs}$. [DBA] according to eq 13, are listed also in Table I.
3. Estimate of $\phi_{T S}{ }^{A}$ from the Fluorescence Decay Curves. Only the values of $\lambda_{\mathrm{a}}$ and $\lambda_{\mathrm{b}}$ have been used thus far to estimate most of the rate constants of Scheme I. From the amplitude ratios $\alpha$ and $\beta$ and the previously calculated values of $k_{2}$ (eq 4) for a series of solutions of cyclohexanone ( 0.076 M ), DBA ( $1.06 \times 10^{-4} \mathrm{M}$ ), and varying concentrations of mesitylene, one can use eq 8 and


Figure 4. Plot of $\left(\lambda_{\mathrm{a}}+\lambda_{\mathrm{b}}\right)$ vs. DBA concentration, according to eq A32. Cyclohexanone concentration $=0.076 \mathrm{M}$, mesitylene concentration $=$ 0.35 M , in cyclohexane at $20^{\circ} \mathrm{C}$. Slope is $(9.7 \pm 0.8) \times 10^{9} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, intercept is $(9.5 \pm 0.3) \times 10^{6} \mathrm{~s}^{-1}$ (linear regression through all points, $r=0.988$ ).

9 to calculate the ratio, $\phi_{T s}{ }^{\mathrm{E}} / \phi_{\mathrm{TS}}{ }^{\mathrm{A}}$, of the coefficients of energy transfer from triplet alkanone and exciplex to DBA ( $\mathrm{S}_{1}$ ), since $k_{\mathrm{ET}}{ }^{\mathrm{E}}, k_{\mathrm{ET}}{ }^{\mathrm{A}}$, and $k_{\mathrm{EA}}$ have been obtained before. Figure 5 is a plot of $Z$ (eq 9) vs. [B]. The slope was obtained by least-square treatment of the data at $[\mathrm{B}]<0.8 \mathrm{M}$, i.e., at values of $-\beta<0.9 .{ }^{10}$ From this slope one can calculate $\phi_{T S} \mathrm{E} / \phi_{\mathrm{TS}}{ }^{\mathrm{A}} \simeq 7$. Furthermore $k_{\mathrm{A}}$ and thus $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}$ (eq 6) can now be derived from eq 10 . On the basis of the results obtained at $[\mathrm{B}] \leq 0.8 \mathrm{M}$, one gets $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}=0.011$ $\pm 0.002$.
This result can be compared to a more direct and independent determination of $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}$ (eq 14) from the fluorescence decay curves of solutions of cyclohexanone and DBA ( $0.5-7.2 \times 10^{-4} \mathrm{M}$ ) without mesitylene. These experiments gave $\phi_{\mathrm{TS}}{ }^{\mathrm{A}}=0.01-0.02$. The agreement is encouraging.

## Discussion

The DBA method is uniquely able to reveal the formation of an excited transient during the decay of photoexcited cyclohexanone in the presence of mesitylene. The assignment of this

[^3]

Figure 5. Dependence of $Z$, as defined by eq 8 , on the concentration of mesitylene. Cyclohexanone concentration $=0.077 \mathrm{M}, \mathrm{DBA}$ concentration $=1.05 \times 10^{-4} \mathrm{M}$, in degassed cyclohexane at $20^{\circ} \mathrm{C}$. The leastsquares analysis was carried out on data points obtained at [B] $<0.8 \mathrm{M}$; see text; slope $=9.0 \times 10^{7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$.
transient to a triplet exciplex of the ketone and the aromatic is the simplest hypothesis. The key observations which support it can be summarized as follow:
(a) DBA fluorescence slowly builds up to a second maximum after most of the prompt fluorescence has decayed. No second peak and no intensity anomalies are observed in the absence of a benzene derivative; on the other hand, in the absence of ketone the fluorescence of DBA decays always as a single exponential, with or without the aromatic.
(b) Delayed fluorescence has a higher integrated intensity when even low concentrations of an aromatic are present in the ketone/DBA solution. Thus the transient species generated is capable of transferring electronic energy to DBA.
(c) Acetonitrile can replace cyclohexane as the solvent without seemingly affecting much the exciplex peak observed with cyclohexanone and mesitylene (one experiment at 0.28 M ). Therefore the transient is not related to the photoreduction of the excited alkanone by cyclohexane, or to any other reaction involving this solvent.
(d) Singlet excited alkanone is obviously not directly involved; it undergoes intersystem crossing long before the exciplex peak appears.

The validity of the exciplex assumption is confirmed by the very good internal consistency between the predictions based on it (the kinetic expressions derived from Scheme I) and the experimental results. Figure 1 illustrates how well the decay of fluorescence intensity, followed over five decades, can be fitted to a triple exponential function, as the mechanism requires. Such a large dynamic range is indeed one of the major advantages of emission techniques compared to methods based on absorption spectroscopy. The use of a large number of channels, here 4096 , in the time-to-pulse-height analysis allows for excellent time resolution. Table I shows convincingly that several of the rate constants of Scheme I can be obtained by different routes with very satisfactory agreement in most cases. Thus, the DBA method allows for the determination of all the rate constants of Scheme I.

Regarding the triplet exciplex dynamics, the following points are particularly significant:
(1) The rate of exciplex formation $k_{\mathrm{EA}}$ appears to be orders of magnitude slower than $k_{\text {diff }}$. This may indicate significant energy or entropy restrictions for the formation of the exciplex from a loose encounter complex

$$
\mathrm{A}+\mathrm{B} \underset{k_{\text {diff }}}{\stackrel{k_{\text {dif }}}{\rightleftharpoons}} \mathrm{A} . . \mathrm{B} \rightleftharpoons \mathrm{E}
$$

as suggested in the case of the proposed triplet excimers of naphthalene and of 1 -chloronaphthalene, the phosphorescence of which was reported by Takemura et al. ${ }^{11}$
(2) At $20^{\circ} \mathrm{C}$, the equilibrium constant, $K_{\mathrm{E}}=k_{\mathrm{EA}} / k_{\mathrm{AE}} \simeq 13$ (between $\sim 10$ and $\sim 50$ ), favors the exciplex.
(3) In the absence of DBA, the lifetime of the postulated exciplex of triplet cyclohexanone and mesitylene is half that of the uncomplexed triplet akanone ( $k_{\mathrm{d}}{ }^{\mathrm{E}} \simeq 2{k_{\mathrm{d}}}^{\mathrm{A}}$ ).
(4) The overall rate constants for energy transfer to DBA ( $k_{\mathrm{ET}} \mathrm{A}^{\mathrm{A}}$ and $k_{\mathrm{ET}}{ }^{\mathrm{E}}$ ) are $\leqslant k_{\text {diff }}$, as expected for a collisional TT transfer (see below).

Turning now to the efficiency of the process of energy transfer from triplet donor to DBA which results in the population of the $S_{1}$ state of DBA, it is intriguing to find that, in this unusual TS sensitization, the exciplex is a significantly better donor than the uncomplexed ketone, since $\phi_{\mathrm{Ts}}{ }^{\mathrm{E}} \simeq 7 \phi_{\mathrm{Ts}}{ }^{\mathrm{A}}$. However, this result was not unexpected, having been obtained previously in the case of the more unstable triplet exciplex of acetone and benzene. ${ }^{3 a}$ As proposed then, a possible interpretation invokes a better match of energy levels between the triplet exciplex and a higher triplet ( $\mathrm{T}_{n}$ ) of DBA. It is indeed likely, although still unproven, that one or several such $T_{n}$ states of DBA, known to be located only a few kilocalories above DBA $\left(\mathrm{S}_{1}\right)$, play an important intermediary role in the overall TS energy transfer, as follow:

$$
\begin{array}{r}
{ }^{3} \mathrm{~A}^{*}\left(\text { or }{ }^{3} \mathrm{E}^{*}\right)+\operatorname{DBA}\left(\mathrm{S}_{0}\right) \rightarrow \\
\mathrm{A}(\text { or } \mathrm{A}+\mathrm{B})+\operatorname{DBA}\left(\mathrm{T}_{n}\right) \rightarrow \mathrm{DBA}\left(\mathrm{~S}_{1}\right)
\end{array}
$$

Evidently other factors besides energy levels may determine $\phi_{\mathrm{TS}}$, among them, for example, the size of the donor and the delocalization of its triplet energy. ${ }^{12}$

Extension of this work is under way along different directions. The effects of temperature and solvent may help ascertain the origin of the low rates of exciplex formation (enthalpy or entropy factors?) and the role of charge-transfer interactions in the binding of the exciplex. The effects of substitution on the alkanone and the aromatic are also being investigated.

## Appendix

Derivation of Eq 1-10. Pulse excitation at time $t=0$ by monochromatic light absorbed by both A and DBA produces $\left[\mathrm{A}^{*}\right]_{0}$ and $\left[\mathrm{DBA}^{*}\right]_{0}$. The asterisks denote triplet excitation of the alkanone and of the exciplex and singlet excitation of DBA; i.e., $\mathrm{A}^{*}$ stands for ${ }^{3} \mathrm{~A}^{*}$ (intersystem crossing is assumed to be fast and efficient ${ }^{5}$ ), $\mathrm{E}^{*}$ stands for ${ }^{3} \mathrm{E}^{*}$, and $\mathrm{DBA}^{*}$ for ${ }^{1} \mathrm{DBA}^{*}$. Only reactions A1 to A11 need be considered.

$$
\begin{align*}
& \mathrm{A}+h \nu \rightarrow \mathrm{~A}^{*}  \tag{Al}\\
& \mathrm{DBA}+h \nu \rightarrow \mathrm{DBA}^{*}  \tag{A2}\\
& \mathrm{~A}^{*} \xrightarrow{k_{\mathrm{d}}^{\mathrm{A}}} \mathrm{~A}  \tag{A3}\\
& \mathrm{~A}^{*}+\mathrm{B} \xrightarrow{k_{\mathrm{EA}}} \mathrm{E}^{*}  \tag{A4}\\
& \mathrm{~A}^{*}+\mathrm{DBA} \xrightarrow{\phi_{T \mathrm{~S}} \mathrm{~A}_{\mathrm{EI}}{ }^{\mathrm{A}}} \mathrm{DBA}^{*}+\mathrm{A}  \tag{A5}\\
& \mathrm{~A}^{*}+\mathrm{DBA} \xrightarrow{\left(1-\phi_{T S^{A}}\right) k_{E T}^{A}} \text { DBA }  \tag{A6}\\
& \mathrm{E}^{*} \xrightarrow{k_{\mathrm{AE}}} \mathrm{~A}^{*}+\mathrm{B} \tag{A7}
\end{align*}
$$

$$
\begin{align*}
& \mathrm{E}^{*}+\mathrm{DBA} \xrightarrow{\phi_{\mathrm{TS}}{ }^{\mathrm{E}} k_{\mathrm{ET}}{ }^{\mathrm{E}}} \mathrm{DBA}^{*}+\mathrm{A}+\mathrm{B} \tag{A8}
\end{align*}
$$

(11) (a) Takemura, T.; Aikawa, M.; Baba, H.; Shindo, Y. J. Am. Chem. Soc. 1976, 98, 2205. (b) For other examples of rates of triplet exciplex formation slower than $k_{\text {diff }}$, see for example: ref 1 b and Caldwell, R. A., Sovocol, G. W.; Gajewski, R. P. Ibid. 1973, 95, 2549. (c) For a general discussion of $k_{\text {diff }}$ and rate of exciplex formation, see: Lewis, C.; Ware, W. R. Mol. Photochem. 1973, 5, 261.
(12) In a personal communication (1982) Brian Stevens proposes an alternative mechanism for diffusional T-S energy transfer. It involves formation of a triplet exciplex of the ketone and DBA. Energy transfer would take place within this exceiplex, with or without concomitant intersystem crossing in DBA to give DBA $\left(S_{1}\right)$, promoted by the bromine atoms. A decision regarding these alternative mechanisms must await new experimental evidence. We thank Prof. Stevens for this interesting suggestion.

$$
\begin{gather*}
\mathrm{E}^{*}+\mathrm{DBA} \xrightarrow{\left(1-\phi_{\mathrm{TS}}^{\mathrm{E}}\right) k_{\mathrm{EI}}^{\mathrm{E}}} \mathrm{DBA}+\mathrm{A}+\mathrm{B}  \tag{A10}\\
\mathrm{DBA}^{*} \xrightarrow{k_{\mathrm{F}}} \mathrm{DBA}+h \nu_{\mathrm{F}} \tag{A11}
\end{gather*}
$$

The rate expressions are

$$
\begin{gather*}
\mathrm{d}\left[\mathrm{~A}^{*}\right] / \mathrm{d} t=-k_{1}\left[\mathrm{~A}^{*}\right]+k_{\mathrm{AE}}\left[\mathrm{E}^{*}\right]  \tag{A12}\\
\mathrm{d}\left[\mathrm{E}^{*}\right] / \mathrm{d} t=k_{\mathrm{EA}}[\mathrm{~B}]\left[\mathrm{A}^{*}\right]-k_{2}\left[\mathrm{E}^{*}\right]  \tag{A13}\\
\mathrm{d}\left[\mathrm{DBA}^{*}\right] / \mathrm{d} t=k_{\mathrm{A}}\left[\mathrm{~A}^{*}\right]+k_{\mathrm{E}}\left[\mathrm{E}^{*}\right]-k_{\mathrm{F}}\left[\mathrm{DBA}^{*}\right] \tag{A14}
\end{gather*}
$$

where

$$
\begin{gather*}
k_{1}=k_{\mathrm{EA}}[\mathrm{~B}]+k_{\mathrm{ET}}^{\mathrm{A}}[\mathrm{DBA}]+k_{\mathrm{d}}^{\mathrm{A}}  \tag{3}\\
k_{2}=k_{\mathrm{AE}}+k_{\mathrm{ET}}^{\mathrm{E}}[\mathrm{DBA}]+k_{\mathrm{d}}^{\mathrm{E}}  \tag{4}\\
k_{\mathrm{A}}=\phi_{\mathrm{Ts}}{ }^{\mathrm{A}} k_{\mathrm{ET}}[\mathrm{DBA}]  \tag{6}\\
k_{\mathrm{E}}=\phi_{\mathrm{TS}}{ }^{\mathrm{E}} k_{\mathrm{ET}}^{\mathrm{E}}[\mathrm{DBA}] \tag{7}
\end{gather*}
$$

To find the solutions of the differential equations A12-A14, one tries the following solutions

$$
\begin{gathered}
{\left[\mathrm{A}^{*}\right]=a_{1} e^{-\lambda t}} \\
{\left[\mathrm{E}^{*}\right]=a_{2} e^{-\lambda t}} \\
{\left[\mathrm{DBA}^{*}\right]=a_{3} e^{-\lambda t}}
\end{gathered}
$$

The time-dependent $e^{-\lambda t}$ factors out and one gets a set of homogeneous, linear, simultaneous, first-order algebraic equations in $a_{1}, a_{2}, a_{3}$ with parameter $\lambda$ :

$$
\begin{gather*}
\left(\lambda-k_{1}\right) a_{1}+k_{\mathrm{AE}} a_{2}=0  \tag{A15}\\
k_{\mathrm{EA}}[\mathrm{~B}] a_{1}+\left(\lambda-k_{2}\right) a_{2}=0  \tag{A16}\\
k_{\mathrm{A}} a_{1}+k_{\mathrm{E}} a_{2}+\left(\lambda-k_{\mathrm{F}}\right) a_{3}=0 \tag{A17}
\end{gather*}
$$

Since these equations are homogeneous, one can only get the values of the ratios of variables, such as $a_{2} / a_{1}$ or $a_{3} / a_{1}$, and therefore there is an extra equation. But one will get consistent solutions only for certain values of $\lambda$, such that the determinant A18

$$
\left|\begin{array}{lll}
\lambda-k_{1} & k_{\mathrm{AE}} & 0  \tag{A18}\\
k_{\mathrm{EA}}[\mathrm{~B}] & \lambda-k_{2} & 0 \\
k_{\mathrm{A}} & k_{\mathrm{E}} & \lambda-k_{\mathrm{F}}
\end{array}\right|=0
$$

of the coefficients of the variables is zero. This is a cubic equation in $\lambda$, which has three roots, $\lambda_{a}, \lambda_{b}, \lambda_{c}$. The determinant A18 can also be written

$$
\left(\lambda-k_{F}\right)\left|\begin{array}{ll}
\lambda-k_{1} & k_{\mathrm{AE}} \\
k_{\mathrm{EA}}[\mathrm{~B}] & \lambda-k_{2}
\end{array}\right|=0
$$

One solution is $\lambda-k_{F}=0$, or

$$
\begin{equation*}
\lambda_{c}=k_{F} \tag{A20}
\end{equation*}
$$

The other two solutions are the roots of the quadratic equation

$$
\begin{equation*}
\lambda^{2}-\left(k_{1}+k_{2}\right) \lambda+k_{1} k_{2}-k_{\mathrm{EA}} k_{\mathrm{AE}}[\mathrm{~B}]=0 \tag{A21}
\end{equation*}
$$

These two roots are

$$
\begin{align*}
& \lambda_{\mathrm{a}, \mathrm{~b}}= \\
& (1 / 2)\left(k_{1}+k_{2}\right) \pm(1 / 2) \sqrt{\left(k_{1}+k_{2}\right)^{2}-4 k_{1} k_{2}+4 k_{\mathrm{EA}} k_{\mathrm{AE}}[\mathrm{~B}]} \tag{A22}
\end{align*}
$$

which rearranges to

$$
\begin{equation*}
\lambda_{\mathrm{a}, \mathrm{~b}}=(1 / 2)\left(k_{1}+k_{2}\right) \pm(1 / 2) \sqrt{\left(k_{1}-k_{2}\right)^{2}+4 k_{\mathrm{EA}} k_{\mathrm{AE}}[\mathrm{~B}]} \tag{2}
\end{equation*}
$$

For each of the three values $\lambda_{a}, \lambda_{b}$, and $\lambda_{c}$ of $\lambda$, a nontrivial solution of eq A15, A16, and A17 giving the ratios such as $a_{2} / a_{1}$ and $a_{3} / a_{1}$ can be obtained. One generates three sets of equations, A23a,b,c, A24a,b,c, and A25a,b,c, by substituting $\lambda=\lambda_{a}, \lambda=\lambda_{b}, \lambda=\lambda_{c}$, respectively, in eq A15, A16, and A17. In eq A23, where $\lambda=$ $\lambda_{\mathrm{a}}$, the coefficients will be called $a_{1}, a_{2}$, and $a_{3}$; in eq A24, with $\lambda=\lambda_{b}$, the coefficients are $b_{1}, b_{2}, b_{3}$, etc., as follow:

$$
\begin{gather*}
\left(\lambda_{\mathrm{a}}-k_{1}\right) a_{1}+k_{\mathrm{AE}} a_{2}=0  \tag{A23a}\\
k_{\mathrm{EA}}[\mathrm{~B}] a_{1}+\left(\lambda_{\mathrm{a}}-k_{2}\right) a_{2}=0  \tag{A23b}\\
k_{\mathrm{A}} a_{1}+k_{\mathrm{E}} a_{2}-\left(\lambda_{\mathrm{a}}-k_{\mathrm{F}}\right) a_{3}=0  \tag{A23c}\\
\left(\lambda_{\mathrm{b}}-k_{1}\right) b_{1}+k_{\mathrm{AE}} b_{2}=0  \tag{A24a}\\
k_{\mathrm{EA}}[\mathrm{~B}] b_{1}+\left(\lambda_{\mathrm{b}}-k_{2}\right) b_{2}=0  \tag{A24b}\\
k_{\mathrm{A}} b_{1}+k_{\mathrm{E}} b_{2}-\left(\lambda_{\mathrm{b}}-k_{\mathrm{F}}\right) b_{3}=0  \tag{A24c}\\
\left(\lambda_{\mathrm{c}}-k_{1}\right) c_{1}+k_{\mathrm{AE}} c_{2}=0  \tag{A25a}\\
k_{\mathrm{EA}}[\mathrm{~B}] c_{1}+\left(\lambda_{\mathrm{c}}-k_{2}\right) c_{2}=0  \tag{A25b}\\
k_{\mathrm{A}} c_{1}+k_{\mathrm{E}} c_{2}-\left(\lambda_{\mathrm{c}}-k_{\mathrm{F}}\right) c_{3}=0 \tag{A25c}
\end{gather*}
$$

Thus, one has three sets of solutions for the original three differential eq A12-A14. Any linear combination of these three solutions with any coefficients is also a solution. The general solutions are the sums of three exponentials:

$$
\begin{align*}
{\left[\mathrm{A}^{*}\right] } & =a_{1} e^{-\lambda_{a} t}+b_{1} e^{-\lambda_{b} t}+c_{1} e^{-\lambda_{c} t}  \tag{A26}\\
{\left[\mathrm{E}^{*}\right] } & =a_{2} e^{-\lambda_{a} t}+b_{2} e^{-\lambda_{b} t}+c_{2} e^{-\lambda_{c} t}  \tag{A27}\\
{\left[\mathrm{DBA}^{*}\right] } & =a_{3} e^{-\lambda_{a} t}+b_{3} e^{-\lambda_{b} t}+c_{3} e^{-\lambda_{g} t} \tag{A28}
\end{align*}
$$

where $c_{1}=c_{2}=0$ (no [DBA*] term in eq A12 and A13) and $\lambda_{c}$ $=k_{\mathrm{F}}$, the fastest of the three rates, of independently known value. Hence

$$
\begin{equation*}
I_{\mathrm{t}}=\alpha e^{-k_{\mathrm{F}} l}+\beta e^{-\lambda_{\mathrm{a}} l}+e^{-\lambda_{\mathrm{b}} l} \tag{1}
\end{equation*}
$$

where

$$
\begin{equation*}
a_{3} / b_{3}=\beta \tag{A29}
\end{equation*}
$$

(which has a negative value)

$$
\begin{equation*}
c_{3} / b_{3}=\alpha \tag{A30}
\end{equation*}
$$

From the difference between $\lambda_{\mathrm{a}}$ and $\lambda_{\mathrm{b}}$ (eq 2), one obtains expressions for $k_{1}$ and $k_{2}$ (eq 5). The sum and product of $\lambda_{\mathrm{a}}$ and $\lambda_{b}$ lead to two other useful expressions, eq A31 and A32:

$$
\begin{aligned}
& \lambda_{\mathrm{a}} \lambda_{\mathrm{b}}=k_{\mathrm{ET}}{ }^{\mathrm{A}} k_{\mathrm{ET}} \mathrm{E}[\mathrm{DBA}]^{2}+\left(k_{\mathrm{ET}}{ }^{\mathrm{A}} k_{\mathrm{AE}}+k_{\mathrm{ET}}{ }^{\mathrm{A}} k_{\mathrm{d}}{ }^{\mathrm{E}}+\right. \\
& \left.k_{\mathrm{d}}{ }^{\mathrm{A}} k_{\mathrm{ET}}{ }^{\mathrm{E}}\right)[\mathrm{DBA}]+k_{\mathrm{EA}} k_{\mathrm{d}}^{\mathrm{E}}[\mathrm{~B}]+k_{\mathrm{EA}} k_{\mathrm{ET}} \mathrm{E}[\mathrm{~B}][\mathrm{DBA}]+ \\
& k_{\mathrm{d}}{ }^{\mathrm{A}}\left(k_{\mathrm{AE}}+k_{\mathrm{d}}^{\mathrm{E}}\right)(\mathrm{A} 31)
\end{aligned}
$$

$\lambda_{a}+\lambda_{b}=$
$\left(k_{\mathrm{ET}}{ }^{\mathrm{A}}+k_{\mathrm{ET}}{ }^{\mathrm{E}}\right)[\mathrm{DBA}]+k_{\mathrm{EA}}[\mathrm{B}]+k_{\mathrm{d}}{ }^{\mathrm{A}}+k_{\mathrm{d}}{ }^{\mathrm{E}}+k_{\mathrm{AE}}$
At $t=0$, the boundary conditions of eq A26, A27, and A28 are

$$
\begin{gather*}
{\left[\mathrm{A}^{*}\right]_{0}=a_{1}+b_{1}}  \tag{A33}\\
{[\mathrm{E}]^{0}=a_{2}+b_{2}=0}  \tag{A34}\\
{\left[\mathrm{DBA}^{*}\right]_{0}=a_{3}+b_{3}+c_{3}} \tag{A35}
\end{gather*}
$$

Since the ketone and DBA are in a homogeneous solution, they absorb the light in any small volume element in this solution in proportion to their extinction coefficients and partial concentrations. Thus,

$$
\begin{equation*}
R=\left[\mathrm{DBA}^{*}\right]_{0} /\left[\mathrm{A}^{*}\right]_{0}=\epsilon_{\mathrm{DBA}}[\mathrm{DBA}] / \epsilon_{\mathrm{A}}[\mathrm{~A}] \tag{11}
\end{equation*}
$$

Based on this definition of $R$, on the values of $\alpha$ and $\beta$ (eq A29 and A30), and on the boundary conditions (eq A33-A35), two new expressions (eq 9 and 10) can be derived as follow, with

$$
\begin{equation*}
Z=k_{\mathrm{E}} k_{\mathrm{EA}}[\mathrm{~B}] / k_{\mathrm{A}} \tag{8}
\end{equation*}
$$

One can write

$$
\begin{equation*}
\frac{b_{3}}{a_{3}}=\frac{b_{3}}{b_{2}} \frac{b_{2}}{a_{2}} \frac{a_{2}}{a_{3}} \tag{A36}
\end{equation*}
$$

and calculate each ratio separately.
From eq A23b:

$$
\begin{equation*}
\frac{a_{1}}{a_{2}}=\frac{k_{2}-\lambda_{\mathrm{a}}}{k_{\mathrm{EA}}[\mathrm{~B}]} \tag{A37}
\end{equation*}
$$

Dividing eq A 23 c by $a_{2}$ and replacing $a_{1} / a_{2}$ by its value above:

$$
\frac{a_{3}}{a_{2}}=\left\{k_{\mathrm{A}} \frac{\left(k_{2}-\lambda_{\mathrm{a}}\right)}{k_{\mathrm{EA}}[\mathrm{~B}]}+k_{\mathrm{E}}\right\} \frac{1}{k_{\mathrm{F}}-\lambda_{\mathrm{a}}}
$$

With eq 8 , this becomes

$$
\begin{equation*}
\frac{a_{2}}{a_{3}}=\frac{k_{\mathrm{EA}}[\mathrm{~B}]\left(k_{\mathrm{F}}-\lambda_{\mathrm{a}}\right)}{k_{\mathrm{A}}\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)} \tag{A38}
\end{equation*}
$$

The boundary condition (eq A34) gives

$$
\begin{equation*}
\frac{b_{2}}{a_{2}}=-1 \tag{A39}
\end{equation*}
$$

From eq A24b, one gets

$$
\begin{equation*}
\frac{b_{1}}{b_{2}}=\frac{k_{2}-\lambda_{\mathrm{b}}}{k_{\mathrm{EA}}[\mathrm{~B}]} \tag{A40}
\end{equation*}
$$

Dividing eq A 24 c by $b_{2}$, and replacing $b_{1} / b_{2}$ by its value above, one has

$$
\frac{b_{3}}{b_{2}}=\left\{k_{\mathrm{A}} \frac{\left(k_{2}-\lambda_{\mathrm{b}}\right)}{k_{\mathrm{EA}}[\mathrm{~B}]}+k_{\mathrm{E}}\right\} \frac{1}{k_{\mathrm{F}}-\lambda_{\mathrm{b}}}
$$

or

$$
\begin{equation*}
\frac{b_{3}}{b_{2}}=\frac{k_{\mathrm{A}}\left(k_{2}-\lambda_{\mathrm{b}}+Z\right)}{k_{\mathrm{EA}}[\mathrm{~B}]\left(k_{\mathrm{F}}-\lambda_{\mathrm{b}}\right)} \tag{A41}
\end{equation*}
$$

Using eq A38, A39, and A41, eq A36 can now be rewritten

$$
\begin{equation*}
\frac{b_{3}}{a_{3}}=-\frac{\left(k_{\mathrm{F}}-\lambda_{\mathrm{a}}\right)\left(k_{2}-\lambda_{\mathrm{b}}+Z\right)}{\left(k_{\mathrm{F}}-\lambda_{\mathrm{b}}\right)\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)} \tag{A42}
\end{equation*}
$$

In these experiments with cyclohexanone and mesitylene, $k_{\mathrm{F}} \gg$ $\lambda_{a, b}$. Thus, eq A42 can be further simplified to

$$
\begin{equation*}
Z=\frac{\left(k_{2}-\lambda_{\mathrm{a}}\right)+\beta\left(k_{2}-\lambda_{\mathrm{b}}\right)}{1+\beta} \tag{9}
\end{equation*}
$$

From the boundary conditions, eq A33 and A34, one calculates $R$, as defined by eq 11 :

$$
R=\frac{a_{3}+b_{3}+c_{3}}{a_{1}+b_{1}}
$$

which rearranges to

$$
\begin{equation*}
R\left(\frac{a_{1}}{a_{3}}+\frac{b_{1}}{a_{3}}\right)=1+\frac{1}{\beta}+\frac{c_{3}}{a_{3}} \tag{A43}
\end{equation*}
$$

Since $b_{2} / a_{2}=-1$ (eq A39)

$$
\begin{equation*}
\frac{a_{1}}{a_{3}}+\frac{b_{1}}{a_{3}}=\frac{a_{1}}{a_{2}} \frac{a_{2}}{a_{3}}-\frac{b_{1}}{b_{2}} \frac{b_{2}}{a_{2}} \frac{a_{2}}{a_{3}}=\frac{a_{2}}{a_{3}}\left(\frac{a_{1}}{a_{2}}-\frac{b_{1}}{b_{2}}\right) \tag{A44}
\end{equation*}
$$

Using eq A37, A38, and A40, this equation becomes

$$
\begin{equation*}
\frac{a_{1}}{a_{3}}+\frac{b_{1}}{a_{3}}=\frac{\left(k_{\mathrm{F}}-\lambda_{\mathrm{a}}\right)\left(\lambda_{\mathrm{b}}-\lambda_{\mathrm{a}}\right)}{k_{\mathrm{A}}\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)} \tag{A45}
\end{equation*}
$$

The ratio $c_{3} / a_{3}$ in eq A43 can be written

$$
\frac{c_{3}}{a_{3}}=\frac{c_{3} b_{3}}{b_{3}} \frac{a_{3}}{a_{3}}
$$

or, from the definitions of $\alpha$ and $\beta$ (eq A29 and A30)

$$
\begin{equation*}
\frac{c_{3}}{a_{3}}=\frac{\alpha}{\beta} \tag{A46}
\end{equation*}
$$

With eq A45 and A46, eq A43 becomes

$$
\frac{R\left(k_{\mathrm{F}}-\lambda_{\mathrm{a}}\right)\left(\lambda_{\mathrm{b}}-\lambda_{\mathrm{a}}\right)}{k_{\mathrm{A}}\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)}=1+\frac{1+\alpha}{\beta}
$$

In these experiments $k_{\mathrm{F}} \gg \lambda_{\mathrm{a}}$ and $\alpha \gg 1$; therefore

$$
\frac{k_{\mathrm{F}} R\left(\lambda_{\mathrm{b}}-\lambda_{\mathrm{a}}\right)}{k_{\mathrm{A}}\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)}=\frac{\alpha}{\beta}
$$

or

$$
\begin{equation*}
k_{\mathrm{A}}=\frac{\beta k_{\mathrm{F}} R\left(\lambda_{\mathrm{b}}-\lambda_{\mathrm{a}}\right)}{\alpha\left(k_{2}-\lambda_{\mathrm{a}}+Z\right)} \tag{10}
\end{equation*}
$$

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Registry No. Cyclohexanone, 108-94-1; mesitylene, 108-67-8; 9,10dibromoanthracene, 523-27-3; cyclohexanone-mesitylene complex, 89891-17-8.

# The Use of Mixed Crystals for Engineering Organic Solid-State Reactions: Application to Benzylbenzylidenecyclopentanones 

Charis R. Theocharis, ${ }^{\text {1a }}$ Gautam R. Desiraju, ${ }^{\text {lb }}$ and William Jones*la<br>Contribution from the Department of Physical Chemistry, University of Cambridge, Lensfield CB2 1EP, England, and the School of Chemistry, University of Hyderabad, P.O. Central University, Hyderabad 500 134, India. Received July 8, 1983


#### Abstract

The concept of chloro/methyl group interchange as a tool in crystal engineering is discussed with respect to derivatives of 2-benzyl-5-benzylidenecyclopentanone (1-4). A study of the mixed crystals containing either $\mathbf{1}$ and 2 (X) or 3 and 4 (Y) demonstrates that molecules which otherwise crystallize into photostable crystal structures may be incorporated into a light-sensitive form. Furthermore, such mixed crystals are demonstrated (using four-circle diffractometry) to undergo single-crystal $\rightarrow$ single-crystal reaction with the formation of the product dimer molecules identified within the reactant lattice. The final $R$ for X is 0.0418 , for Y it is 0.0578 , and for irradiated X it is 0.0394 .


It is clear that the controlled variation of the substituent groups present on an organic molecule may allow subsequent crystalli-
zation into particular and desired packing arrangements ${ }^{2}$. One particular strategy for this so-called crystal-engineering concept


[^0]:    ${ }^{\dagger}$ Department of Chemistry, Northeastern University, Boston, MA 02115.

[^1]:    (1) Triplet exciplexes of metalloporphyrins and anthracene (but see ref 1c) with nitro aromatics or chloro compounds have been reported from flash spectroscopy data: (a) Roy, J. K.; Carroll, F. A.; Whitten, D. G. J. Am. Chem. Soc. 1974, 96, 6349. (b) Kapinus, E. I.; Aleksankina, M. M.; Dilung, I. I. J. Photochem. 1983, 21, 125. (c) Kuzmin, V. A.; Renge, I. V.; Borisevich, Yu. E. Chem. Phys. Lett. 1980, 70, 257.
    (2) See, for example: Gupta, A.; Hammond, G. S. J. Am. Chem. Soc. 1976, 98, 1218 . Farid, S.; Hartman, S. E.; Doty, J. C.; Williams, J. L. R. Ibid. 1975, 97, 3697. Caldwell, R. A.; Creed, D. Acc. Chem. Res. 1980, 13, 45. Cohen, S. G.; Parola, A.; Parsons, G. H. Chem. Rev. 1973, 73, 141. Loufty, R. O.; Yip, R. W. Can. J. Chem. 1973, 51, 1881. Scaiano, J. C.; Perkins, M. J.; Sheppard, J. W. J. Photochem. 1983, 21, 137. Ulrich, T.; Steiner, U. E.; Föll, R. E. J. Phys. Chem. 1983, 87, 1873 and references therein.

[^2]:    (3) (a) Wilson, T.; Halpern, A. M. J. Am. Chem. Soc. 1980, 102, 7279. (b) Ibid. 1981, $103,2412$.
    (4) (a) Vassil'ev, R. F. Nature (London) 1963, 200, 773. Belyakow, V. A.; Vassil'ev, R. F. Photochem. Photobiol. 1970, 11, 179. (b) Wilson, T.; Halpern, A. M. J. Am. Chem. Soc. 1980, 102, 7272 and references therein. (c) For a discussion of quenching experiments to reveal exciplex formation, see, for example: Kuzmin, M. G.; Sadowskii, N. A.; Soboleva, I. V. J. Photochem. 1983, 23, 27 and references therein.
    (5) Murov, S. L. "Handbook of Photochemistry"; Marcel Dekker: New York, 1973.
    (6) For the details of the derivation of the equations below, see Appendix.

[^3]:    (10) With the straight line constrained to go through the origin.

